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The Alleviation of Coordination Problems through Financial Risk Management*

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Abstract

We characterize a firm as a nexus of activities and projects with their associated cashflow distributions across states of the world and time. With specialized managers intent on maximizing firm value, we show that such a representation leads to a transformation possibility frontier between the riskiness and expected value of cashflows. A firm reacts to changes in the market prices of risks by adjusting its value maximizing portfolio of real activities. We show that financial risk management can help to alleviate the reorganization and coordination problems related to the implementation of the desired adjustments. Empirically, we show that a firm’s use of financial derivatives is linked to its reactivity to variations in risk prices. We also argue that financial risk management allows a firm to maintain its value in the presence of cashflow-at-risk or value-at-risk constraints.

JEL Classification: G22, G31, G34

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1 Introduction

The modern view of risk management is financial in nature and does not involve operations despite the fact that enterprise risk management has become a central element of firm operations. In this paper we propose a characterization of the firm where both risk and operations management specialists aim to maximize firm value somewhat independently, as discussed for instance in Hart and Moore (2005). Changes in market conditions create a need for coordination between the two specialists that can only be done at a cost. We argue here that for a firm to maintain its optimal value following changes in the market price of risks, the use of financial instruments can help lower the coordinations costs between the firm’s specialists.

We consider the firm as a nexus of projects and activities that give rise to a distribution function of cashflows across states of nature and time. In the spirit of a mean-variance world used in basic portfolio management theory, we derive an efficient frontier representing the firm’s set of feasible projects and activities in a space with the expected value and riskiness of cashflows as coordinates. In this context, we adopt the view that the production and operations manager (POM) aims mainly at raising the expected value of cashflows whereas the real risk manager (RRM) has as a main objective to reduce the riskiness of cashflows, thereby impacting the selection of projects and activities that give rise to the distribution of cashflows. The financial risk manager (FRM) invests in fair-valued financial instruments that have no direct bearing on the real activities of the firms. This simplified structure captures, albeit in a much stylized way, characteristics of modern corporations: the pervasive presence of specialists in firms as in Hart and Moore (2005), the limited control of business units managers as in Dessein et al. (2005), and the decentralized functional authority framework as in Roberts (2004).

Given market conditions, all feasible combinations of projects and activities can be valued to identify the combination that maximizes firm value. As a result, firm value is determined by the portfolio of projects and activities (from now on “projects”) and the market risk factor prices. As market prices of risk change, a firm must adjust its portfolio of projects, thereby changing its aggregate distribution of cashflows, to achieve a new optimal position on its transformation possibility frontier. Depending on the shape of this frontier, the adjustments will be more or less pronounced. Movement towards the new optimal combination of projects may lead to disagreements between specialized functional managers or business units (here POM and RRM), stemming from the different specific objectives that POM and RRM are typically asked to pursue. We will show how such disagreements underwrite the use of financial instruments as a conflict resolution tool, thereby giving the financial risk manager a role as facilitator, if not coordinator, within the firm. Indeed, using financial instruments may provide important savings in view of the potentially high costs of aligning incentives among managers and business units and/or engaging
in expensive reorganizations.\footnote{1}{Following discussions with senior executives of corporate sponsors of \textit{CIRANO}, an interuniversity research centre on the analysis of organizations, including Bell Canada, Alcan, Hydro-Québec, Royal Bank of Canada and Bombardier, we were comforted in the idea that coordination problems associated with major strategic activities, decisions and investments were tackled by high-level committees involving senior executives from different business units, firm-wide management functions and board representatives. A consensus must be reached before the reviewed investments, actions and changes in activities can be pursued and implemented. Similar issues are also highlighted in \textit{The Renewed Finance Function - Extending Performance Management Beyond Finance}, CFO Research Services, CFO Publishing Corporation, November 2007.} As usual, we find in our context that, in the absence of market inefficiencies, there is no role for financial risk management since investors could undo any financial transaction by a firm so that firm value is then independent of the financial risk management strategy (Titman 2002).\footnote{2}{Smith and Stulz (1985) and Jin and Jorion (2006) discuss a hedging irrelevance proposition similar to the leverage irrelevance theorem of Modigliani and Miller (1958): A firm cannot create value by hedging risks since investors bear the same cost of risk as the firm. This characteristic is present in our context as well.}

Our setup establishes a clear link between the use of financial instruments and changes in market parameters, namely the risk free rate, the volatility of the risk factor return and the expected risk premium. We derive the prediction that the use of financial instruments will be more pronounced when the transformation possibility frontier (between the riskiness and expected value of cashflows) of a firm is weakly concave since a small movement in the market parameters will then lead to important adjustments in the firm’s optimal portfolio of projects. A test of our theory will therefore be to relate the use of financial instruments, in particular the use of financial derivative instruments, by a firm to the concavity measure of its specific frontier.

To find such empirical support for our theory, we collected a panel of accounting, financial and risk management data for 269 large U.S. firms for the years 1993 to 2004. We first construct for each firm a measure of the propensity of its efficient frontier to react to a change in the market price of risk by taking the annual change in the position in terms of mean and riskiness of cashflows. Using this measure, we first show that there is a strong relationship at the industry level between the level of reactivity and the use of financial derivative instruments. Second, using a ranked probit approach at the firm level, we find that reactivity has a sizable and statistically significant positive impact on the number of operational risks that a firm manages using financial derivatives. This result holds even after controlling for other variables traditionally expected to have a significant impact on the use of financial derivative instruments. Our empirical results are consistent with our contention that financial risk management may contribute indirectly to enhance firm value by alleviating the coordination problems between the different firm functions and divisions associated with changes in the portfolio of projects.\footnote{3}{The trade-off between specialization benefits and coordination costs and the impact of such trade-off on organizational structure have been noted by many authors. See among others Becker and Murphy (1993), Bolton and Dewatripont (1994), Boyer and Robert (2006).}

The transformation possibility frontier captures implicitly both technological and strategic characteristics of a firm. Our representation therefore captures the ability of a firm to change
its risk characteristics through changes in its portfolio of projects, that is, to increase its value, through those changes, by decreasing its cashflow beta (Stulz 2004) or by increasing it if doing so allows sufficiently higher expected cashflows. For instance, pursuing the idea that malleability in production could allow a firm to reduce its fixed expenses, Mackay and Moeller (2006) have linked the concavity of revenues with respect to output prices to the use of risk management instruments. In the same spirit, we relate a firm’s reactivity with respect to the market prices of risk to its use of financial derivative products. Hence, in a world with no taxes, no bankruptcy or financial distress costs, and no agency conflicts between the different classes of stakeholders, there still exist a value-adding role for financial risk management as a relatively inexpensive coordination tool favoring congruence of interests in the firm.

Stulz (2004) provides a systematic review of the various theoretical justifications for risk management within a firm. Taxes, financial distress costs and/or agency costs are needed to justify hedging in a value-maximizing firm. A firm facing a convex tax schedule increases its value by reducing, through risk management, the variability of its taxable earnings. Hedging can lower the expected cost of financial distress by reducing the probability of unfavorable outcomes. Also, if hedging makes earnings less volatile, it lessens the information asymmetry and reduces agency costs. Several other reasons are found in the literature. Risk management can facilitate optimal investment and add value to a firm by favoring more stable free cashflows when the cost of external financing is higher than the cost of funding projects internally. Hedging may help retain valuable large shareholders or get stakeholders to make firm-specific investments.

The remainder of the paper is organized as follows. We present the model of the efficient frontier and the value of a firm in Section 2. Section 3 discusses the reactivity of firms to changes in the market price of risk and captures the coordination problems that may emerge between RRM and POM. It stresses the important role that financial risk management can play in alleviating these coordination problems. In Section 4, we conduct an empirical study to investigate the link between the use of financial instruments and the concavity of the transformation possibility frontier. Section 5 extends the analysis to related issues. We conclude in Section 6.

2 The firm as a portfolio of projects

“(In the late 1990s) ABB was made up of some 1300 operating companies, each with its own income statement and balance sheet... (which) in turn contained 5000 profit centers. Each operating company was matrixed under a dual reporting relationship... a country head... (and) a global product area executive... Both bosses had a say in performance evaluations and compensation.” D. John Roberts (2004), p.110.

2.1 Preliminaries

A firm is defined as a nexus of projects representing all real activities, such as those related to investment and production, and giving rise to a transformation possibility frontier for cashflows. This frontier is the envelope of all feasible vectors of cashflows over states of nature and time periods obtainable from all projects characterizing and identifying the firm as an economic entity. Hence, it accounts for all human, technological, contractual, legal and other constraints facing a firm. In the short term, a firm can modify its overall distribution of cashflows over states and time periods and switch from one distribution to another within its feasibility set by changing its project portfolio. In the long term, a firm can modify its feasibility frontier by changing constraints underlying the transformation possibility set, generally through technological and organizational innovations such as mergers, acquisitions and divestitures, or innovation and patent initiation.

If a firm can change its operations or increase its flexibility to significantly reduce its risk without changing expected cashflows, its market value will increase as the given expected cashflows will be discounted at a lower rate. Rather than characterizing a firm by a quasi-fixed and exogenously given risk measure, we see a firm as choosing, within its feasibility set, a portfolio of projects to obtain a distribution of cashflows that maximizes its value given the market prices of risk. We therefore approach risk management from the general viewpoint of the economics of the firm rather than from the usual financial perspective, in the spirit of the early contributions of Fama and Miller (1972) and Cummins (1976). We summarize the activities of a firm through the generated cashflows over states of nature and time periods.

To set ideas, we characterize in Figure 1 a firm by two blocks, real asset management and financial risk management. The first block is broken down into production and operations management (POM) on one hand, and real risk management (RRM) on the other. All activities within a firm, such as project selection or self-protection, can be described along these two dimensions. Financial risk management is purposely set apart and involves all transactions carried out through the purchase or sale of financial instruments.
We first show how to construct the efficient frontier for a firm. This will involve the choice of a risk model to characterize the trade-offs between expected cashflows and risk. For simplicity, we start with a linear factor model, valid period by period, where all sources of risk are priced. We then establish how to calculate the value of a firm. It will involve deriving an optimal portfolio of projects given the market prices of risk factors.

2.2 The possibility frontier and the market prices of risk factors

A firm is a technology by which cashflows \( cf_{st} \) related to various projects \( p \in \{1,2,\ldots,P\} \) defining a firm as an economic entity are distributed over or transformed between different states \( s \) and periods \( t \), with \( s \in \{1,2,\ldots,S\} \) and \( t \in \{1,2,\ldots,T\} \), under technological, legal, or contractual constraints. The transformation possibility frontier of firm \( j \) (i.e., the envelope of all feasible cashflow vectors) given its information set \( \Omega_0 \) at time \( t = 0 \) can be represented as

\[
G_j (cf_{11}, \ldots, cf_{st}, \ldots, cf_{ST} \mid \Omega_0) = 0, \tag{1}
\]

where \( cf_{st} \) is the aggregate cashflow over all projects \( p \) in state \( s \) and period \( t \). The envelope of all feasible cashflow vectors is concave.

A firm modifies cashflows through changes in its portfolio of projects. Characteristics of the vector of aggregate cashflows lead to the firm’s evaluation by financial markets. Given its technological possibilities represented by (1), a firm chooses the mix of POM and RRM activities to reach the vector of aggregate cashflows that maximizes its value. Hence, the frontier \( G_j (\cdot) = 0 \) must be understood as the frontier that emerges from the POM and RRM activities. We later discuss the representation of financial risk management activities in this framework.

For presentation clarity, we now describe a multifactor model with \( N \) orthogonal risk factors so that their mutual covariances are zero. We also assume, for simplicity, constant expected cash flows per period, \( E_s(cf_{st}) = E_j, \forall t \), and an infinite number of periods. The rate at which these constant expected cashflows should be discounted is given by:

\[
ER_j = R_F + \sum_{i=1}^{N} \beta_{ji} (ER_i - R_F) \tag{2}
\]

where \( ER_i \) is the expected return on risk factor \( i \), \( R_F \) is the risk free rate, and \( \beta_{ji} \) is the measure of risk with respect to the \( i \)-th factor. In such a setting, firm value is simply:

\[
V_j = \frac{E_j}{ER_j}. \tag{3}
\]
Expressed in terms of cashflows, the security market line or hyperplane (2) takes the form:

\[ E_j = V_j ER_j = V_j R_F + \sum_{i=1}^{N} V_j \beta_{ji} (ER_i - R_F), \]  
\[ (4) \]

where \( V_j \beta_{ji} \) measures the risk of the firm’s cashflows with respect to the \( i \)-th factor:

\[ V_j \beta_{ji} = V_j \frac{COV(R_j, R_i)}{Var(R_i)} = \frac{COV(V_j R_j, R_i)}{Var(R_i)} = \frac{COV(cf_j, R_i)}{\sigma_i^2} = \rho_{ji} \frac{\sigma_{cf_j}}{\sigma_i}, \]  
\[ (5) \]

where \( \sigma_{cf_j} \) measures the volatility of the firm’s cashflows and \( \sigma_i \) measures the volatility of the market return on the \( i \)-th risk factor. We can rewrite (4) as

\[ E_j = V_j R_F + \sum_{i=1}^{N} \rho_{ji} \sigma_{cf_j} \left( \frac{ER_i - R_F}{\sigma_i} \right), \]  
\[ (6) \]

or

\[ V_j = \frac{1}{R_F} \left[ E_j - \sum_{i=1}^{N} \rho_{ji} \sigma_{cf_j} \left( \frac{ER_i - R_F}{\sigma_i} \right) \right]. \]  
\[ (7) \]

The value of a firm depends, in this context, only on \( E_j \) and the scaled correlations \( SCOR_{ji} = \rho_{ji} \sigma_{cf_j} \) between a firm’s cashflows and market returns on the different risk factors.

Relative to valuing a firm, the variables \( E_j \) and \( SCOR_{ji} \equiv \rho_{ji} \sigma_{cf_j}, \ i \in \{1, 2, \ldots, N\} \) are \( N+1 \) sufficient statistics of all projects within a firm. The transformation possibility frontier (1) can therefore be rewritten in terms of \( E_j \) and \( SCOR_{ji} \) as the envelope of all feasible points:

\[ H_j (E_j, SCOR_{j1}, \ldots, SCOR_{jN}) = 0. \]  
\[ (8) \]

We will work with this representation of a firm’s technology.\(^5\)

Defining a firm’s feasibility set in terms of expected cashflows \( E_j \) and the \( N \) scaled correlation values \( SCOR_{ji} \) has several advantages. First, it allows the value of RRM and POM activities to be measured from their capacity to move a firm toward or along the frontier \( H_j(\cdot) = 0 \) in the \((E_j, SCOR_{j1}, \ldots, SCOR_{jN})\)-space. A change in the mix of POM and RRM activities will usually generate a change of value. Second, it allows proper aggregation of risks at the firm level by establishing a functional relationship between risk factors and cashflows for the many projects or business units. Identifying risk factors that are common to the various projects and accounting for the dependencies between them is an important function in a firm, which can fall under the

\(^5\)To draw the efficient frontier for a given firm, one needs the set of cashflows associated with the numerous projects defining the firm as a business entity along with the scaled correlations between the firm’s cashflows and the returns on risk factors. Although the collection of such data is no small task, firms do undertake it, at least at some level of aggregation.
responsibility of a central unit or delegated to various units. The identification and measurement
tasks are important functions of the chief operations officer, the chief risk officer and the chief
executive officer.

2.3 The value of the firm

The value of a firm is generated by a mix of POM and RRM activities. For simplicity, one may
represent POM (resp. RRM) as being intent on maximizing expected cashflows (resp. minimizing
scaled correlations) for given scaled correlations of a firm’s cashflows (resp. expected cashflows)
with the $N$ different risk factor returns. Both activities thus contribute to the overall objective of
maximizing value. In reality, these functions are often diffuse in an organization and sometimes
shared by the same division. In this context, the primary responsibility of higher level executives
is to ensure that a firm’s decision making process brings it on its frontier.

For further simplicity, let us assume that there is a single risk factor, namely the market
portfolio risk. This will allow us to develop the main ideas in a simple graphical fashion. With
$SCOR_{jM} = p_j M \sigma_{cfj}$, we can write (6) and (7) as:\(^6\)

\[
E = VR_F + V \beta (ER_M - R_F) = VR_F + SCOR_M \left( \frac{ER_M - R_F}{\sigma_M} \right),
\]
\[
V = \frac{1}{R_F} \left[ E - SCOR_M \left( \frac{ER_M - R_F}{\sigma_M} \right) \right].
\]

From (9), we observe that $\beta \leq \left[ \frac{E - SCOR_M \left( \frac{ER_M - R_F}{\sigma_M} \right)}{VR_F} \right]$ as $SCOR_M \leq \left[ \frac{E - SCOR_M \left( \frac{ER_M - R_F}{\sigma_M} \right)}{VR_F} \right] V \sigma_M$. We can illustrate the problem of a
firm in the $(E, SCOR_M)$-space as in Figure 2, where each dot represents a potential project with
a $(E, SCOR_M)$ pair of coordinates. All projects a firm can undertake are represented in that
space where the frontier is constructed as the minimum level of risk obtainable for a given level
of expected cashflows (see Merton, 1972).

[Insert Figure 2]

We can represent iso-value lines as in Figure 3. By definition, an iso-value line represents
combinations of $E$ and $SCOR_M$ giving the same market value. From (10), iso-value lines are
linear and parallel, with slope equal to the market price of risk

\[
\theta_M = \frac{E(R_M) - R_F}{\sigma_M}
\]

[Insert Figure 3]

\(^6\)We will drop the index of firm $j$ when the context is clear and no confusion is possible.
The value $V$ attached to a given iso-value line can be obtained by discounting the zero-$SCOR$ expected cashflow level ($C_1$ and $C_2$ in Figure 3) at the risk-free rate $R_F$: $V_1 = C_1/R_F$, $V_2 = C_2/R_F$. Firm value increases in the North-West direction.

The combination of expected cashflows ($E$) and scaled correlation between cashflows and market returns ($SCOR_M$) that maximizes firm value is the combination at which the efficient frontier reaches the highest iso-value line. For that combination (point $A_2$ on Figure 3), the usual tangency condition holds:

**Proposition** To maximize its value, a firm must equate its marginal rate of substitution, the rate at which it can substitute POM and RRM activities while remaining on its efficient frontier, to the market price of risk:

$$-rac{\partial (OM)}{\partial (RM)} = -\frac{\partial E}{\partial SCOR_M (cf_j, R_M)} \bigg|_{H(E,SCOR_M)=0} = \frac{E (R_M) - R_F}{\sigma_M}.$$

At $A_2$ on Figure 3, a firm cannot reduce its scaled correlation without reducing expected cashflows. At point $A_1$, however, the scaled correlation can be reduced without affecting expected cashflows because point $A_1$ is not located on the efficient frontier. A firm’s POM and RRM strategies and policies are not efficient if they bring it to a situation such as point $A_1$. By better managing its real risk to reduce the scaled correlation of its cashflows, or by better managing operations to increase expected cashflows, a firm is able to increase its value. In this framework, the firm is assumed to maximize its value. Given that financial markets care about expected returns and risk, so does the firm. In so doing, the firm is not risk averse but rather sensitive to the way markets evaluate cashflow distribution over states of nature and periods.

It is obvious that a N-factor linear model will be an immediate extension to the single risk factor model we just described. A firm will maximize its value at the point of tangency between an efficient hyper-frontier and the highest reachable iso-value hyperplane. In Section 5, we also discuss how to account for unpriced risk factors and sketch a general intertemporal risk model. For the purpose of illustrating the role of financial risk management and motivating our empirical application relating the efficient frontier to hedging activities, we will maintain a simple one-factor risk model.

### 3 Firm Value and Financial Instruments

Developments in the previous sections dealt mainly with real asset management. This section covers the role of financial risk management. Our main argument will be that financial risk management is a relatively inexpensive way to respond to changes in market conditions. Changes in the price of risk alter the portfolio of projects and activities that maximizes firm value; this cre-
ates coordination problems that the financial risk manager can alleviate. Although the necessary changes in the portfolio of projects are the same with or without the presence of a financial risk manager, his presence allows the firm to achieve these changes at a lower coordination cost. When the market price of risk changes, the extent by which a firm’s portfolio of projects must change depends on the distance between the old and the new portfolio of projects. If the efficient frontier is relatively flat, the change in the optimal portfolio involves a rather important reshuffling of projects. On the opposite, a less important change is needed if the frontier is more concave. The precise measure of the reactivity of the firm to changes in the market price of risk will be discussed in the next section.

Whereas the transaction costs associated with financial instruments are low, coordinating changes in real operations through the implementation of new projects or the abandonment of existing ones typically entails substantial costs. Moving from one optimal portfolio of projects to another involves a complex set of trade-offs in terms of increasing or reducing cashflows and increasing or reducing risk among the many organizational units of a firm, each mixing production and operations management activities and real risk management activities. Several cashflows-at-risk or value-at-risk constraints may also be imposed at various levels in an organization. We argue through a simple graphical illustration that financial risk management reduces the cost of implementing the desired changes in real operations. As a result, firms that are more flexible are more likely to use financial derivatives to make real adjustments less costly.

To understand and model these complex interrelationships, one needs to rely on the general theory of decentralization in hierarchies and on the theory of incentives under incomplete information. As evident in Mookherjee (2006), the theory of incentives has ignored so far the decentralization of risk management objectives. Moreover, aggregation of VaR targets in the risk management literature raises difficulties even abstracting from incentive issues.

To develop our argument while avoiding an unnecessarily complex modeling of the structural interactions in organizations, we assume a separation of objectives between real risk management, intent on reducing the SCOR value (that is, favoring projects that contribute to that goal), and production and operations management, intent on increasing the E value. Conflicts may therefore appear: the real risk manager will tend to oppose changes that increase the riskiness of cashflows (SCOR) whereas the production and operations manager will tend to oppose changes that reduce expected cashflows (E). Such a representation of the conflict between RRM and POM functions is admittedly extreme. It nevertheless characterizes in a simplified way the difficulties encountered

7In large corporations bonuses are usually linked to cashflow performance targets and less so to risk measures. Even option-based compensation rewards managers for cashflow performance to the possible detriment of real risk management activities. With respect to the compensation of real risk managers, Gable and Sinclair-Desgagné (1997) and Sinclair-Desgagné (1999) offer an audit-like procedure to assess managerial performance in the context of environmental (real) risk management and control. An excellent cashflow performance of a manager may be penalized if the audit procedure reveals that it has been achieved to the detriment of proper risk management.
when various managers need to coordinate their choices to maximize value. As mentioned above, major investments and policy or strategy decisions must typically gather a relatively large consensus among managers, executives and board members before being undertaken.\(^8\) We sketch below the coordination problems between RRM and POM in this simplified setting.

### 3.1 Value creating coordination

Suppose, for some reason, that a firm finds itself at a point on its efficiency frontier to the left of the optimal mix of POM and RRM activities as represented by point \(A_1\) in Figure 4.

[Insert Figure 4]

If the POM manager continues trying to increase \(E\) for a given \(SCOR\), while the RRM manager keeps working to reduce \(SCOR\) for a given \(E\), the firm as a whole finds itself trying to move in an infeasible North-West direction. The way out of this efficient but not value maximizing combination of POM and RRM activities is for the RRM manager to let the \(SCOR\) increase above its current level, providing the POM manager with some leeway to increase \(E\). In so doing, the RRM manager must momentarily destroy value, by letting \(SCOR\) increase given \(E\), giving the POM manager the flexibility to ultimately increase firm value. The same argument can be developed for point \(A_2\). In this case the POM manager must let \(E\) decrease below its current level. In so doing, the POM manager must momentarily destroy value to give the RRM manager the possibility to reduce \(SCOR\), thereby create value. In both instances, it is necessary for one manager to destroy firm value initially to allow the other manager enough room to eventually create more value. This level of coordination is clearly difficult as the former manager must assume some career risk.

### 3.2 Firm reactivity and value creation through financial risk management

We have thus far posited that in our framework with no taxes, no financial distress costs, no transaction costs of bankruptcy, and no agency problems, value is created within a firm only through its choice of real projects and activities.\(^9\) This means that maximal value is created only through an optimal mix of real activities, blending both POM and RRM ones. As the market price of risk changes, the optimal \(E - SCOR\) combination of cashflows also changes, thus generating significant coordination problems. We will now show that financial risk management creates value by alleviating these coordination problems.

\(^8\)One can also think of coordination problems as being driven by organizational inertia, which emerges as different groups (or management functions) acquire quasi-veto rights on some changes in the activities of a firm. See Hannan and Freeman (1984) and Boyer and Robert (2006).

\(^9\)This statement is clearly reminiscent of Proposition III in Modigliani and Miller (1958, page 288): “... the cut-off point for investment in the firm ... will be completely unaffected by the type of security used to finance the investment.”
Consider Figure 5. Suppose a firm’s optimal mix is initially at \( A_2 \) but because of a change in the market price of risk, the new optimal mix is at \( A_0 \). Suppose, moreover, that the POM manager is unwilling or unable to destroy positive net present value projects (moving down) to provide the RRM manager with enough flexibility to reach point \( A_0 \). How can financial risk management help in this process?

Consider the iso-value line that goes through point \( A_2 \). This line is, by definition, lower than the iso-value line tangent to the possibility frontier at point \( A_0 \). The slope of iso-value lines is the price of risk, that is, the price at which one can exchange risk, SCOR, for expected cashflows \( E \) on financial markets. Therefore, under conditions of perfect financial markets and in a manner similar to an individual’s portfolio choice under the two-fund separation approach, a firm can enter into financial transactions to move from \( A_2 \) to any point on the same iso-value line. These movements, for example to point \( B \), are done at no cost, by assumption, but do not affect firm value since financial transactions are not creating value per se.

The advantage of moving a firm’s \((E, \text{SCOR})\) combination to point \( B \) is that the RRM and POM managers are then given the mandate to move the firm from \( B \) to \( A_0 \). What then is the value of financial risk management? In and of itself, the value is zero. Its value comes from the fact that it reduces the coordination costs to attain a new mix of risk and expected cashflows. Moving from \( A_2 \) to \( A_0 \) requires abandoning [accepting] some projects with positive [negative] net present value given the SCOR-coordinate at \( A_2 \), hence the normal opposition of the POM manager to those changes. Similarly, moving from \( A_1 \) to \( A_0 \) requires abandoning [accepting] some projects that are risk reducing [increasing] given the \( E \)-coordinate at \( A_1 \), hence the natural opposition of the RRM manager to those changes. But given the new \( E \) and SCOR coordinates at \( B \), the real changes in the project mix to move the firm from \( B \) to \( A_0 \) can now be agreed upon by both managers: the real changes are the same but they can be achieved at lower coordination costs.

4 Empirical evidence on the link between firm reactivity and hedging

Assuming that a firm can gather all the necessary information about future cashflows associated with its numerous projects, current and future, and given a risk model, it can construct at any time the type of efficiency frontier we have described in the previous sections. Obviously, this is not an easy and straightforward task. We analyze some of the difficulties in section 5.2 below. It is much harder to gather a panel of such data sets for several firms. Therefore, to test some implications of our characterization of the firm, we must adopt an indirect approach.

\(^{10}\)Similarly, if we start at point \( A_1 \), the RRM manager is unwilling to create risk and destroy value to give the POM manager enough flexibility to reach point \( A_0 \).
The important empirical implication of our theory is that more reactive firms, having less concave possibility frontiers, will want to adjust their \((SCOR, E)\) position by larger margins when the market price of risk changes. Figure 7 illustrates our point.

[Insert Figure 7]

A firm whose possibility frontier is more concave will react less to changes in the market price of risk (moving typically from point \(A\) to point \(B_{low}\) in Figure 7) and therefore will need little change in its portfolio of projects and activities. On the other hand, a firm whose possibility frontier is less concave will see its optimal project mix change more (typically from point \(A\) to point \(B_{high}\)).

Our empirical analysis will proceed in two steps. First, we propose a measure of firm reactivity to risk price changes. Then, we want to link this reactivity to the use of financial derivatives since more reactive firms should be heavier users of financial risk management products to alleviate coordination costs associated with large changes in their portfolio of projects.

4.1 Data Set Construction

We build our data set starting from the 500 firms making up the Standard and Poor’s 500 index. For all firms present in the index over the period 1993-2004, we gather annual accounting information and stock market information from annual Reports, Compustat, Bloomberg and CRSP, as well as derivative usage and managerial shareholding and option ownership from the EDGAR US Database. We provide in an appendix a list of all data items required for our empirical analysis with their source\(^{11}\). Not all data items were available for all firms over the sample period. In the end, we were left with 269 companies.

The distribution of firms across industries is given in Table 1. The manufacturing sector represents a large proportion of the total but this will not bear a significant weight on the results of our main analysis based on individual firms as long as there is enough cross-sectional variation in the reactivity of manufacturing firms. we will see that it is indeed the case.

4.2 Measuring Reactivity and the Use of Financial Derivatives

To compute the reactivity factor, we first measure the annual change \(\Delta P_{jt}\) in a firm \(j\) position in the \((SCOR, E)\)-space by the Euclidian distance between the firm positions in two adjacent years, scaled by the firm market value \(V_{jt}\) to control for size, that is:

\[
\Delta P_{jt} \equiv \sqrt{(SCOR_{jt} - SCOR_{jt-1})^2 + (CF_{jt} - CF_{jt-1})^2}/V_{jt}
\]

\(^{11}\)A longer appendix providing more details is available from the authors upon request.
where $SCOR_{jt} = V_{jt} \ast \sigma_{Mt} \ast \beta_{jt}$, with $\sigma_{Mt}$ being the volatility of market returns at time $t$, computed historically over the last two hundred trading days, and $\beta_{jt}$ being firm $j$’s market beta in period $t$.

We then run a linear regression of the change in a firm’s position ($\Delta P_{jt}$) on the annual change in the market price of risk ($\Delta \theta_t$) over the period 1993-2004, that is:

$$\Delta P_{jt} = \alpha_j + \gamma_j \Delta \theta_t + \varepsilon_{jt}$$

where $\Delta \theta_t = \theta_t - \theta_{t-1}$, with $\theta_t$ given by (11). The regression coefficient $\gamma_j$ is our measure of reactivity for firm $j$. Notice that it is an average measure over the sampling period that defines the structural characteristic of a firm.

For the use of financial derivatives, researchers have most often used a dichotomous variable that takes the value 1 when the firm uses derivatives and 0 when it does not. This variable would leave us with two little cross-sectional variation between firms to identify the link between reactivity and use of derivatives. In our data set, we managed to collect use of derivatives for four types of risks for each firm. In the EDGAR database, as defined by US regulations, firms report hedging for equity risk, commodity risk, exchange rate risk, and interest rate risk. The first three are considered operational and the last one financial. Attributing a (0,1) variable for each type of risk we can now count the number of risks a firm hedges. This is the variable we will use for our analysis.

To study the link between the reactivity measure we have constructed and this measure for the use of financial derivatives we will proceed first at an aggregate industry level. The idea will be to determine whether the more reactive industries hedge more risks. Then we will run a multivariate ordered probit with the number of risks as a dependent variable at the firm level to establish whether reactivity enters as a significant explanatory variable over and above the usual variables used to explain the hedging behavior of firms.

We will conduct our analysis for the cross-section of firms in 2004, the end-point of our sample. This will prevent to some extent endogeneity issues since the $\gamma_i$, the reactivity measures, are computed over a ten-year period (1993-2004) and all the other variables will take the value in the cross-section of 2004.

### 4.3 Estimation of the link between reactivity and hedging

Before assessing the link between reactivity and the use of financial derivatives at the firm level we want to see if our hypothesis gets some empirical support at the industry level. To perform the analysis, we use the industry categories of Table 1. The non-classified refers in fact to conglomerates, which are known to be heavy users of financial derivatives. We then add this reference
category to see how it ranks in terms of reactivity.

### 4.3.1 Industry level analysis

We compute a given industry’s reactivity by the $V_i$-weighted average of reactivity measures $\gamma_j$ (from regressions 13) of the firms in that industry. To compute the aggregate use of derivatives by an industry, we use four 0-1 variables indicating whether in 2004 a firm hedges or not a given risk, whose sum gives the number of risks hedged by a given firm. We then take the weighted average of those numbers, where the weights are the ratios of the market values of the firms over the total market value of the industry.

Table 2 presents the ranking of the twelve industries in terms of their estimated reactivity level $\gamma$, from the most reactive (Utilities) to the least reactive (Construction). The other columns of the table show the market-value weighted average number of operational risks (equity, commodity, and foreign exchange) that firms in that industry manage through the use of derivative contracts as well as the average number of total risks (operational plus interest rate) managed. The six most reactive industries (Utilities to Service) are those that are the top users of financial derivative contracts to manager operational risks. Although the ranking differs slightly when we add the use of interest risk derivatives, the same six most reactive industries remain the top six users of derivative contracts.

Figure 8 illustrates graphically the link between average industry reactivity and the average number of operational risks managed (a similar picture is obtained when the total number of risks is used). The linear relationship is of positive slope, which is significant at the five-percent level, and no industry appears in the second and fourth quadrants.

### 4.3.2 Firm level analysis

We now examine the relationship between the estimated reactivity level $\gamma_j$ and the number of operational risks managed at the firm level in 2004. The number of firms in the sample is reduced to 238 as we dropped the 31 firms in the financial industry since some variables (quick ratio, foreign sales and reserves) are not computed in the same way as in other industries. Moreover, financial firms are both users and providers of financial derivatives. Of the firms in the sample, 29.8% use no derivative instrument to manage operational risk, 50% manage only one risk through derivatives, 18.5% two risks, and 1.7% manage all three risks.

We use a ranked probit approach.\footnote{De Angelis and Garcia (2008) show the advantage of such a ranked approach over a simple logit for the use of derivatives or a Heckman-type two-step approach.} The dependent variable is the number of operational risks that a firm manages using derivatives. Therefore, this variable takes the value 0, 1, 2 or 3.
We use the following explanatory variables. First and foremost we want to include the variables that previous studies have used to explain the use of financial derivatives by firms to hedge risk. These include the quick ratio (current assets minus inventories divided by current liabilities), the ratio of foreign sales to total sales, and the carry-forward of net operating losses over the total assets: the higher the first ratio is, the less need there is for a firm to hedge; a firm with significant foreign operations will be subject to currency risk and will therefore be more likely to use foreign exchange derivatives; finally, the last variable measures the tax benefit that can be obtained by carrying forward losses. These three variables are the traditional measures included in hedging studies for leverage, foreign exposure and convexity of the tax schedule.\textsuperscript{13} The fourth traditional variable related to the use of financial derivatives is the size of the firm\textsuperscript{14} and we measure it by the logarithm of the firm assets.

A potential problem with using S&P500 firms is to overweight large firms in the sample. Since large firms tend to use more financial derivatives because of the large fixed cost of using derivatives, one may argue that we lack cross-sectional variation to support reactivity as a reason for hedging due to implicit coordination costs. To address this issue, we control for size in our ordered probit analysis.

Graham and Rogers (2002) argue against the net operating losses as a proxy for measuring the tax benefit and propose a refined measure using the Graham and Smith (1999) approach to explicitly measure tax function convexity. This technique quantifies the convexity-based benefits of hedging by determining the tax savings that result from reducing volatility. Another explanatory variable often used to explain the hedging decision is a ratio of long-term debt to the assets of a firm.\textsuperscript{15} However, it is usually the interest rate risk that is considered when accounting for the tax incentive to hedge by increasing debt capacity.\textsuperscript{16} We include this variable but considering that we do not include the use of interest rate derivatives we do not expect this variable to be significant.

Our purpose is to verify that our reactivity variable still plays a significant role after controlling for the tax benefit effect and that we find a significant effect for net operating losses as in the previous studies using this proxy. This is indeed the case.

We estimate the probit model by maximum likelihood.\textsuperscript{17} The results are reported in Table 3, where a coefficient (together with a p-value) refers to the impact of that variable on the probability that the firm hedges a greater number of operational risks. All four traditional variables above come out with the expected sign and are significant at close to the 5% level, especially after

\textsuperscript{14}See among others Nance et al. (1993).
\textsuperscript{15}See among others Graham and Rogers (2002).
\textsuperscript{16}Graham and Rogers (2002) also find that hedging leads to greater debt capacity.
\textsuperscript{17}A full description of the variables included in the probit is given in the appendix.
controlling for the industry effect. Therefore, our analysis confirms the results in previous studies. More importantly for the purpose of this paper, however, the results in Table 3 show quite clearly that reactivity has a statistically significant positive impact on the number of operational risks managed with financial derivatives. This result, together with the previous ranking of industry reactivity and use of derivatives, supports our hypothesis that a firm’s sensitivity to the market price of risk is a strong determinant of the use of financial derivatives, in addition to the traditional reasons for hedging such as leverage, foreign exposure, convexity of the tax schedule, and size.

To capture the role of financial risk management in alleviating coordination problems we also introduce the number of business segments in a firm\(^{18}\). This is certainly an imperfect measure of coordination problems or costs but it indicates that the hierarchical structure is important over and above the mere size of the firm. Its clear significance reinforces the link between hedging and the complexity of the firm’s activities. We present also results with a control for the industry to which a firm belongs. In this case we prefer not to include business segments.\(^{19}\) The results remain robust and are practically the same as without the control for industry.

We have also included in the probit model other variables that some previous studies have used to explain hedging such as dividend policy, the book-to-market ratio, and the security holdings of the managers in the firm to account for risk aversion in agency frameworks\(^{20}\). None of those is significant at reasonable levels of confidence.

For robustness purposes, we ran a series of other regressions that for space considerations we do not report. We started our investigation by running a simple logit, where we considered only the use or no-use of derivatives as the dependent variable. The usual hedging variables came out with the right sign and were significant except for the net operating losses, while the reactivity variable had the right sign but with a coefficient twice as small and a p-value of 0.35. Obviously accounting for the number of risks adds useful information to the regression to identify the propensity of a firm to use derivatives with more or less intensity\(^{21}\).

We have also tried other measures of reactivity based on the curvature of the frontier instead of the distance between the expected cashflow - risk positions. The results were similar but less significant. Finally, we included the beta of the firms to control for the level of risk but it did not

\(^{18}\)See the appendix for a description of how this variable was constructed

\(^{19}\)The number of segments was collected in the annual reports of the firms. Given how Compustat classifies a company’s industry it would be econometrically unsound to include both the number of business segments and industry control dummies in the same regression. For instance Compustat has one industry category called "non classified" that clearly includes the large conglomerates purely on the basis of the number of business segments. Also there are industries where the choice of business segments is more refined than in other industries and the number of business segments to report is determined by the firm (see Harris, 1998), which induces a systemic bias in the number of business segments across industries.

\(^{20}\)For the determination of managerial shareholding and option ownership, we analysed the portfolio of the top five executives of the firm as in Ofek and Yermack (2000).

\(^{21}\)In a very thorough econometric analysis, DeAngelis and Garcia (2008) show the advantage of using a ranked probit instead of a simple logit with an indicator variable for the use of derivatives.
come out significant.

5 Discussion

In this section we extend the analysis in different directions. We first discuss extensions of the basic risk model, then we point to the problems of acquiring the proper information to draw the efficient frontier, and finally we mention some implications of our analysis from an industrial organization perspective.

5.1 Extensions of the basic risk model

To show that the approach is not limited to the simple risk model analyzed above, we briefly discuss two important extensions. First, we account for the fact that not all risks are priced by the market. This will not prevent the firm from optimizing, as we will explain. Second, and more importantly, we set the trade-offs between expected cashflows and risk in a dynamic framework through a general stochastic discount factor. This formulation will be compatible with many risk model specifications and encompass the linear multifactor model specified in the previous section.

5.1.1 The case of non-valued risks

We have assumed until now that all the risk factors have a market price, so that firm value maximization is achieved at the optimal tangency point between the iso-value hyperplane and the possibility frontier. When the market does not value some risks that are nevertheless taken into consideration by a firm, the valuation problem is different.

We can illustrate this situation with two risk factors: the first is valued by the market and is represented by the market portfolio while the second is managed by the firm at some cost but is diversifiable for an outside investor so that its market value is zero. At what optimal level should a firm manage this non-valued risk? Each level of non-valued risk corresponds to a projected transformation possibility frontier in the space expected value – market-valued risk, namely \( H(E, \text{SCOR}_M \mid \text{SCOR}_{NV}) = 0 \), where \( \text{SCOR}_{NV} \) is the level of non-valued risk taken or assumed by a firm. Under some reasonable assumptions about the non-valued risk (including the existence of a unique global maximum), there is one best or maximal transformation possibility frontier in the space expected value – market-valued risk, namely \( H(E, \text{SCOR}_M \mid \text{SCOR}_{NV}^*) = 0 \). The tangency point between the highest iso-value line and this maximal frontier gives the maximal market value of a firm.

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22 The cross-sectional correlation between the \( \gamma_j \) of the firms and the betas in 2004 was -0.25. We computed this correlation with the betas for other years and always found a negative number of a similar magnitude. One can argue that there should be a negative relation between the beta of a firm and its reactivity factor. A firm that can change its activities easily after a variation in the price of market risk should be less risky.

23 A parallel can be drawn with the production function using a non-valued or zero-cost input, such as water or
5.1.2 An Intertemporal Framework

In the simple risk model we specified earlier, we have sidestepped the problem of computing the present value of intertemporal cashflows by assuming a flat term structure and a constant risk measure over time. Therefore, the transformation possibility frontier did not change over time. In a more realistic setting where risk and return change over time, we need to compute at each point in time, say \( t \), an efficient frontier \( H_t(E_t, SCOR_t) = 0 \), where \( E_t \) and \( SCOR_t \) group all the conditional expected values and scaled correlations. The extension to an intertemporal framework can be set in an Arrow-Debreu type economy or in a world with a general stochastic discount factor. In such intertemporal extensions, the price of risk and the price of time will play a role in the marginal trade-offs the firm will engage in, both across states of nature and periods.

To be as general as possible, we need not specify a linear risk model. We can rely on the existence of a stochastic discount factor, say \( m_{t,T} \), which gives the value in \( t \) of a cashflow in \( T \), in the absence of arbitrage opportunities. The value in \( t \) of any project within a firm with associated cashflows \( C_{t+1}, \ldots, C_T \) from \( t+1 \) to \( T \) is then given by:

\[
P_t = E_t[m_{t,t+1}C_{t+1} + \ldots + m_{t,T}C_T]
\]  

By the covariance formula, we can rewrite this expression as the sum of two distinct blocks, one for products of expectations, the other for covariances:

\[
P_t = EV_t + COV_t
\]  

with:

\[
EV_t = E_t[m_{t,t+1}]E_t[C_{t+1}] + \cdots + E_t[m_{t,T}]E_t[C_T]
\]  

\[
COV_t = Cov_t(m_{t,t+1}C_{t+1}) + \cdots + Cov_t(m_{t,T}C_T)
\]

The expectation terms \( E_t[m_{t,\tau}]_{\tau=t+1}^T \) provide the prices of zero-coupon bonds for corresponding horizons \( \tau = t + 1, \ldots, T \). An efficiency frontier can then be defined in terms of \((E_t, COV_t)\) as before, but now the frontier will change at each period depending on the evolution of the term structure of interest rates and of the risk measures embedded in the stochastic discount factors. Since all quantities have been discounted at time \( t \) accounting for both the values of time and risk in cashflows over time and states of nature the iso-value lines will have a slope of one. Of
course the analysis of the trade-offs between expected cash flows and risk or between different risks becomes more involved but remains possible once a specific content is given to the stochastic discount factor through a model.\textsuperscript{24}

5.2 Caveats on information acquisition

In deriving the transformation possibility frontier between the expected value of projects and their risk, we have assumed away technical or informational issues. Such issues could prevent a chief executive officer from implementing the necessary trade-offs. We will sketch below the main obstacles such as incomplete and asymmetric information, indivisibility and transaction costs.

A first obvious problem is the significant data collection implied by the dimension of the problem. Projects, active and inactive, are numerous in a firm and obtaining the corresponding cashflows over time is no small task. The information collected is also likely to lack precision. Therefore, the frontier may be derived under imprecise and potentially incomplete information, and uncertainty will prevail as to its exact position. This uncertainty will directly affect determination of the optimal mix of production and risk management activities.

A parallel with mean-variance optimization in asset allocation will help us gauge the extent of the problem. It is well known in this literature that small changes in the assumed distribution of asset returns often imply large changes in the optimized portfolio. Many portfolios may be statistically as efficient as the ones on the efficient frontier. Several statistical solutions have been proposed to account for the variability of the efficient frontier (see Michaud, 1998) and to increase the stability of the optimal portfolio (Jagannathan and Ma, 2003). Beyond these statistical solutions, one can mitigate the uncertainty associated with a detailed computation of intertemporal cashflows by aggregating projects among various organizational units. This will make the problem of gathering data generally easier given the accounting system already in place and facilitate the optimization process.

Asymmetric information could also prevent a firm from attaining the project mix that maximizes its value. Adverse selection and moral hazard problems can impede the process of gathering information at every level of a firm’s hierarchy (see Williamson 1967). Managers may propose projects that have been selected on criteria other than maximizing firm value. The collection of projects from which the frontier is drawn may not, therefore, be the right one and the final mix of projects will be suboptimal. Solutions for these problems are the usual incentive schemes that will help elicit the right information.

\textsuperscript{24}When the stochastic discount factor corresponds to the CAPM or the linear multifactor model described in section 2.2, the trade-offs can be expressed between expected cashflows and scaled correlations. To obtain a similar separation of parameters leading to the use of scaled correlations with the general specification in (14), more structure is needed in the stochastic discount factor. For example, one can extend the factor model described earlier to a dynamic factor model where the scaled correlations will change over time, assuming, for simplicity, that the term structure of interest rates is flat.
Another important difficulty in drawing up a possibility frontier for a firm lies in the indivisibility of real assets. In portfolio theory with infinitely divisible financial assets, it is always possible to be arbitrarily close to the efficient point on the frontier. With real activities, some projects must be undertaken completely or not at all. A numerical search for the optimal mix of activities has to proceed differently, but it is still possible to arrive at a frontier. It will not have the smooth appearance that we drew in our graphs but it will keep its optimality property. Similarly, some constraints may be imposed on the minimal size of projects in deriving the optimal frontier.

Transaction costs may explain why a firm does not want to continuously change the optimal mix of projects. For example, premature termination of a project may involve penalties in terms of labor compensation or legal fees. A change in the optimal mix may also be postponed because of fixed costs associated with the disposal of fixed assets. Incorporating these transaction costs in portfolio choice is an extremely difficult theoretical and computational issue. Only partial solutions with specific cost structures, often unrealistic, are available. Transaction costs associated with a change of policy are just one example of sunk or irreversible costs. When a project in underway, managers may induce some changes that will affect its future cashflows; this is another potentially important source of costs.

5.3 An application to VaR and CaR constraints

Another implication of our framework concerns regulatory or self-imposed cashflows-at-risk (CaR) or value-at-risk (VaR) constraints. We show in this section that a firm can, through appropriate financial risk management operations, meet these financial constraints without changing its value maximizing activities and therefore without any impact on its market value. This suggests that, because of the VaR and CaR constraints they face, firms in regulated industries such as financial services and public utilities will be heavier users of derivatives and other financial risk management instruments.

A cashflow-at-risk constraint imposes the requirement that the cashflow shortfall \( E(cf) - cf \) will surpass a desired level \( (CaR) \) with a given probability \( \alpha \): \( \Pr [E(cf) - cf > CaR] = \alpha \). These constraints, when binding, are usually perceived as preventing the maximization of firm value. Every \((E, SCOR)\) combination can be associated with a \( CaR \) value. Iso-CaR curves, that is, curves on which all points have the same \( CaR \) value, can be drawn. On Figure 6, the \( CaR \) value at point \( A_H \) is the same as at point \( D \). Let us identify this curve as \( CaR_H \) and suppose that a firm is required to satisfy that \( CaR_H \) level.

[Insert Figure 6]

A firm’s value is not maximized at point \( A_H \) since the iso-value line through \( A_H \) lies below
the iso-value line through $A_L$, the value maximizing point. The project mix in $A_L$ is certainly attainable given the possibility set of the firm, but $CaR_L$, the iso-$CaR$ curve through point $A_L$, does not satisfy the constraint. As a result, the difference in firm value between $C_L/R_F$ and $C_H/R_F$ represents the cost of the $CaR$ constraint.

With perfect capital markets, a firm is always able to trade zero-value financial contracts at no cost to move along the iso-value line whose slope is the market price of risk. Then, such a movement with financial instruments along the iso-value line going through $A_L$ can bring the firm to point $D$, which satisfies the $CaR$ requirement. At point $D$, firm value is equal to $C_L/R_F > C_H/R_F$ since point $D$ lies on the same iso-value line as $A_L$. Again, value is not created by financial risk management per se. It simply makes a firm obey a $CaR$ constraint while keeping its optimal mix of real activities. This would have been infeasible without the use of financial instruments.

Therefore, $CaR$ constraints should have no impact on the market value of firms under perfect capital markets. Hence, a firm should instruct its real asset managers (POM and RRM) to maximize its value and then ask the financial risk manager to use financial transactions to satisfy the $CaR$ requirement. Consequently, financial risk managers in industries with binding $CaR$ regulation, such as the financial services industry, will use more zero net present value financial contracts that reduce a firm’s risk and expected cashflows (typically from $A_L$ to $D$ in Figure 6) in order to attain the risk-return constraint set by the regulatory body, at no cost in terms of firm value.

5.4 Implications for Industrial Organization Analysis

Despite its arguably abstract nature, our financial and real risk management model leads to several empirical implications for industrial organization analysis. We discuss below some of our results in the context of this literature.

Our empirical analysis shows that firms whose cashflows are more reactive to changes in the market price of risk are more likely to use financial risk management instruments. An interpretation of this result is that the use of financial derivatives facilitates the resolution of coordination problems between line managers, a problem that is more likely to occur when changes in the project mix are important. Our argument thus suggests that multiindustrial and multinational firms, that have a more diverse project mix than single-industry single-country firms, as well as firms with significant growth options, will be heavier users of derivatives.\textsuperscript{25}

Larger corporations are more likely faced with more challenging coordination problems simply because of their wider dispersion of real assets and extensive distribution of responsibilities.\textsuperscript{26}

\textsuperscript{25}Indeed, Geczy et al. (1997) find that firms with extensive foreign exchange-rate exposure (like multinational firms) are more important users of derivatives; He and Ng (1998) maintain the same in the case of conglomerates; and Nance et al. (1993) find that firms with significant growth options use more derivatives.

\textsuperscript{26}With respect to size, for instance, Bodnar et al. (1998), Nance et al. (1993) and Geczy et al. (1997) show that
Indeed, Nance et al. (1997), Mian (1996) and Graham and Rogers (2002) have shown that financial risk management procedures and products, such as forwards, futures, swaps, and options, are more common in larger firms. These empirical regularities contradict theories in which the value of financial risk management is based upon the reduction of the cost of financial distress. Stulz (1996) writes:

“The primary emphasis of the [corporate risk management] theory is on the role of derivatives in reducing the variability of corporate cashflows and, in so doing, reducing various costs associated with financial distress. The actual corporate use of derivatives, however, does not seem to correspond closely to the theory. For one thing, large companies make far greater use of derivatives than small firms, even though small firms have more volatile cashflows, more restricted access to capital, and thus presumably more reason to buy protection against financial trouble. Perhaps more puzzling, however, is that many companies appear to be using [financial] risk management to pursue goals other than variance reduction.”

But these empirical regularities are compatible with the predictions of our model. To justify the greater use of financial derivatives by large firms, previous studies have invoked the large costs of setting up a risk management function. Besides this cost argument, we propose that financial risk management alleviates reorganization and coordination costs, which is a different objective from a variance reduction one. Another test would be to compare corporations where the number of executives who have a say in project approval is large with corporations where that number is small. Because financial risk management is more valuable for corporations that have major coordination problems, our model predicts that firms with a larger number of executives involved in project selection will use more financial risk management techniques. We are not aware of any study on that topic.

Finally, our model leads to a renewed consideration of the use of financial hedging instruments by firms subject to regulated or self-imposed financial constraints, such as value-at-risk or cashflow-at-risk constraints. We showed (Figure 4) that financial risk management could, through the use of zero-value contracts, allow firms to meet those constraints without sacrificing firm value. Larger firms hedge more through the use of derivatives than smaller firms, even though their expected bankruptcy costs are relatively lower. Whereas Block and Gallagher (1986) and Booth et al. (1984) argue that larger firms engage in more financial risk management because of the large fixed costs involved to hedge financial risks, we argue instead that they do so because, relative to smaller firms, they experience more difficult coordination problems. Firms present in more business segments, such as multinational firms and conglomerates that have a more diverse project mix than single-industry single-country firms, will likely experience more important coordination problems, hence should be greater users of derivatives.

27 See also the results from the Wharton-Chase survey (1995) and the Wharton-CIBC Wood Gundy survey (1996) as mentioned in Stulz (1996, page 9): “Whereas 65% of companies with a market value greater than $250 million reported using derivatives, only 13% of the firms with market values of $50 million or less claimed to use them.” See also Boyer and McCormack (2009) for more recent evidence in the manufacturing sector.
Our model suggests therefore that, because they are typically subject to stringent financial constraints of the VaR and CaR types, firms in sectors such as financial services and utilities will be among the heavier users of derivatives and other financial risk management instruments. The reason we elicit here for this significant use of financial risk management procedures and products is clearly different from the standard argument, namely the reduction of financial distress cost.

6 Conclusion

We developed a framework to show that both real and financial risk management can add value to a firm. Contrary to the current academic view of risk management, which makes it a special purpose function of a corporation rather than an integral part of decision making, we proposed a characterization of firms as nexus of projects defined by their expected cashflows and risk, where risk management activities appear alongside operations in maximizing firm value.

We were then able to define a transformation possibility set for a firm. In this context, the object of production and operations management is to raise expected cashflows while real risk management aims to lower risk. By choosing the projects to invest in, managers search for efficiency, that is attaining the frontier of possibilities, as well as for optimality, that is reaching the point on that frontier that maximizes firm value given the market prices of risk factors. Conflicts may arise in the firm when managers, obeying or reacting to different incentive contracts or objectives, do not view the projects as having the same potential contribution to firm value. This is where financial risk management can help a firm in maximizing value.

The facilitating role of financial risk management is crucial whenever changes in the market prices of risk factors induce important changes in the optimal set of projects and activities. Our empirical strategy rests precisely on identifying how much a firm reacts to changes in risk prices: A firm’s reactivity depends on the relative concavity of its possibility frontier. Using time series from 1993 to 2004, we measured this reactivity factor for 269 large U.S. firms. We then related reactivity to the use of financial derivative instruments. First, we found that there is a strong relationship at the industry level between the aggregate measure of reactivity and the use of derivatives. Second, we constructed a probability model at the firm level to explain the number of operational risks managed through financial derivatives. We found a strong and significant role for the reactivity factor in this relation, even after controlling for firm size, leverage, foreign exposure, and the convexity of the tax schedule. We then concluded that the reactivity factor, a measure of the concavity of the possibility frontier, is an important determinant of a firm’s use of financial risk management instruments.

Our interpretation of this relationship is that more reactive firms are likely to face important coordination problems in maximizing their value and that financial risk management facilitates
coordination. It is through such facilitation that financial risk management indirectly contributes to firm value, especially in a context where real asset management activities are decentralized. Our representation of operations and risk management within a firm therefore supports the view that financial risk management can add value even in a world with no taxes, no financial distress costs, and no information asymmetry.

Access to micro data sets on firms could lead to the estimation of risk-reward frontiers, that is, frontiers expressed in terms of risk and expected cashflows. This could lead to a refined analysis of the links between characteristics of the efficient frontier, market parameters and organizational characteristics of the firm. This opens a fascinating new avenue to study the relationship between firm value and risk management.
Appendix - Data Set Description

7.1 Accounting and Market Data

Accounting data included in the database have been extracted from Compustat. Information about betas, risk premium and risk free rate have been extracted from CRSP. Below we describe how each variable was computed from the original items available in Compustat. The numbers refer to the item number in Compustat. A full list of the available items in Compustat is contained in a more complete Appendix available upon request from the authors.

- MV Value: Firm’s market value calculated as the number of shares outstanding times the stock price at fiscal year-end: Data25 × Data199.
- Book Value: Firm’s book value calculated as total assets minus intangibles and total liabilities, (Data6 - Data33 - Data181).
- Div Yield: Dividend paid by share by the stock’s price: Data26 / Data199.
- BV/MV: Firm Market Value / Firm Book Value calculated as Data25×Data199 / (Data6 - Data33 - Data181).
- LT Debt/MV: Firm’s long term debt by its market value, Data9 / Data25 - Data199.
- R&D Expenses: Data46
- Assets: Total assets, Data6
- Liabilities: Total liabilities, Data181
- R&D/Assets: R&D expenses by total assets, Data46 / Data6
- Employees: Data29
- Foreign currency Adj: Foreign currency adjustment, Data150
- Cash: Cash and short-term investment, Data1
- Inventories: Data3
- Current Assets: Data4
- Current Liabilities: Data5
- Quick Ratio: (Current Assets - Inventories) / Current Liabilities × Data4 - Data3 / Data5
- Deferred taxes: Data269 + Data270 + Data271
- Investment tax credit: Data208
- NOL carryforward: Net Operating Losses Carryforward, Data52
- RP: Risk Premium variation calculated as \( X_t - X_{t-1} \)
- SCOR: Calculated as Firm Market Value \( \times \beta \times \sigma_m \)
- E(CF): Firm Cash Flows or Operating earnings before depreciation, Data13
- Shares Outstanding: Number of common shares outstanding at fiscal year-end, Data25
- Stock Price: Price of the common stock at fiscal year-end, Data199
- Capital Ex.: Capital expenditures, Data145

### 7.2 Hedges and Derivative Instruments

Disclosures about hedges and derivatives instruments are included in Item 7a - *Quantitative and Qualitative Disclosure about Market Risk* and in different notes from *Notes to consolidated Financial statements* included in Item 8 Financial Statements and Supplementary Data from the annual report on Form 10-K.

Under Item 7a we found information related to the type of particular market risk and exposures faced by the firm. In addition, we may have found some information about instruments used for hedging. However, fair market value and notional amounts of contracts entered into are usually not disclosed in that section. Still we have looked to this section in order to have a general idea about the hedging policy of the company and the type of risk hedged. If no derivative instruments were contracted during the period covered by the study, it is in this section that we have collected the information.

The greatest part of the data on hedging was collected from the Notes to consolidated Financial statements. Firms reported their derivatives activities for hedging purposes on their annual report through a note on financial instruments or either on a separate note dedicate specifically to hedging instruments and policies. In this type of note on financial instruments we found a description of the type of instrument used and for what purpose (hedging or trading) it was entered into. Subsequently, firms report the carrying value, the fair value and sometimes the notional value of their instruments in accordance with the FASB’s disclosure requirements.

We have looked at derivatives instruments used for four different types of risks:

- Foreign exposure
- Debt and interest rate related
• Commodities

• Equity

We reported the management of such risk with derivatives by a binary variable (1 if the exposure is hedged with derivatives). We also report in the database the aggregate notional (when disclosed), the total fair value of derivatives and finally the fair value of instruments grouped by the type of risk hedged.

While regulation by the FASB about derivatives requires that companies disclosed the type of instruments they use and the fair value of those same instruments, it appears that companies report such use of derivatives in ways that are quite unequal and different. When we could not gather the data at the level of detail we required we did not include the firm in our sample. More details on the method of data collection can be found in examples in a supplementary appendix available upon request from the authors.

7.3 Managerial Ownership

For managerial ownership we collected both stock ownership and options ownership. In order to have information on a comparable basis between firms, we reported the ownership of the top five named executive officers of each firm. Data on beneficial ownership of managers were usually found in the Notice of Annual Meeting of Stockholders (the proxy statement) on form DEF 14A. In this proxy statement, under the section Executive Compensation, companies disclosed the value of unexercised (exercisable and unexercisable) options at fiscal year-end for the CEO and for their five most compensated executive officers. We used this information to calculate the managerial options ownership data. Information regarding stock ownership of management was obtained through the section Information about Beneficial Ownership of Principal Stockholders and Management which is also found on the proxy statement. In this section, firms report the amount and the type of ownership of multiple stockholders. We added the number of stocks that the top five named executive managers hold and multiplied it by the price of the stock at fiscal year-end, which was found either under data item 199 from Compustat or in the proxy statement.

7.4 Business Segments

Data about business segments were collected on the basis of the reportable segments of firms which are subject to regulation from the FASB. SFAS No. 131 Disclosures about Segments of an Enterprise and Related Information requires that a company with publicly traded debt or equity securities report annual and interim financial and descriptive information about its reportable operating segments. Operating segments are components of an enterprise for which separate
financial information is available and such information is evaluated regularly by the chief operating decision maker when deciding how to allocate resources and assess performance.

Segments are generally organized either on the basis of business lines and type of products sold or on a geographic basis in function of the customer’s country or region. Although most firms reported the same number of business segments through the years covered, it is possible that some firms had proceeded to a revision of their reporting segments due for example to acquisitions or discontinuances of operations. Data concerning reportable segments are disclosed in Item 1 of the annual report or in a note on business segments from the Notes to Consolidated Financial Statements under Item 8 of annual report on form 10-K.
References


**Table 1. Distribution of firms across industries**

<table>
<thead>
<tr>
<th>Industry</th>
<th>SIC</th>
<th>Code</th>
<th>Number of firms</th>
</tr>
</thead>
<tbody>
<tr>
<td>Food</td>
<td>2000-2099</td>
<td>1</td>
<td>13</td>
</tr>
<tr>
<td>Mining</td>
<td>1000-1499</td>
<td>2</td>
<td>11</td>
</tr>
<tr>
<td>Construction</td>
<td>1500-1999</td>
<td>3</td>
<td>4</td>
</tr>
<tr>
<td>Manufacturing</td>
<td>2200-3999</td>
<td>4</td>
<td>136</td>
</tr>
<tr>
<td>Transportation</td>
<td>4000-4799</td>
<td>5</td>
<td>5</td>
</tr>
<tr>
<td>Communications</td>
<td>4800-4899</td>
<td>6</td>
<td>4</td>
</tr>
<tr>
<td>Utilities</td>
<td>4900-4999</td>
<td>7</td>
<td>12</td>
</tr>
<tr>
<td>Wholesale</td>
<td>5000-5199</td>
<td>8</td>
<td>4</td>
</tr>
<tr>
<td>Retail</td>
<td>5200-5999</td>
<td>9</td>
<td>25</td>
</tr>
<tr>
<td>Finance</td>
<td>6000-6599</td>
<td>10</td>
<td>31</td>
</tr>
<tr>
<td>Service</td>
<td>7000-9999</td>
<td>13</td>
<td>22</td>
</tr>
<tr>
<td>Non-Classified</td>
<td></td>
<td>14</td>
<td>2</td>
</tr>
</tbody>
</table>
This table reports the weighted average number of risks a firm hedges through the use of financial derivatives by industry as reported in the firms’ 10-K forms. Operational risks include commodity, equity and foreign exchange risks. Interest rate risk is the fourth possible risk that a firm can report being hedge. Industries are classified in decreasing order of their average estimated flexibility level. Flexibility is calculated as the $\gamma_i$ coefficient in the regression $\Delta P_{it} = \alpha_i + \gamma_i \Delta \theta_t + \varepsilon_{it}$, where $\Delta \theta_t$ is the annual variation in the market price of risk and $\Delta P_{it}$ is calculated as $\sqrt{(SCOR_{it} - SCOR_{i,t-1})^2 + (CF_{it} - CF_{i,t-1})^2/V_{it}}$. The rank reports the industry’s decreasing relative position in terms of the number of risks hedged (1 is the greatest user of hedging instruments).

<table>
<thead>
<tr>
<th>Industry</th>
<th>Estimated reactivity level</th>
<th>Weighted number of operational risks hedged</th>
<th>Rank</th>
<th>Weighted number of total risks hedged</th>
<th>Rank</th>
</tr>
</thead>
<tbody>
<tr>
<td>Utilities</td>
<td>0.761</td>
<td>1.206</td>
<td>5</td>
<td>2.111</td>
<td>4</td>
</tr>
<tr>
<td>Food</td>
<td>0.679</td>
<td>1.758</td>
<td>2</td>
<td>2.622</td>
<td>2</td>
</tr>
<tr>
<td>Conglomerates</td>
<td>0.646</td>
<td>2.000</td>
<td>1</td>
<td>3.000</td>
<td>1</td>
</tr>
<tr>
<td>Mining</td>
<td>0.603</td>
<td>1.208</td>
<td>4</td>
<td>2.043</td>
<td>6</td>
</tr>
<tr>
<td>Financial</td>
<td>0.574</td>
<td>1.130</td>
<td>6</td>
<td>2.068</td>
<td>5</td>
</tr>
<tr>
<td>Service</td>
<td>0.551</td>
<td>1.673</td>
<td>3</td>
<td>2.462</td>
<td>3</td>
</tr>
<tr>
<td>Retail</td>
<td>0.508</td>
<td>0.619</td>
<td>9</td>
<td>1.293</td>
<td>10</td>
</tr>
<tr>
<td>Wholesale</td>
<td>0.470</td>
<td>0.163</td>
<td>12</td>
<td>1.030</td>
<td>11</td>
</tr>
<tr>
<td>Manufacturing</td>
<td>0.451</td>
<td>1.028</td>
<td>7</td>
<td>1.609</td>
<td>8</td>
</tr>
<tr>
<td>Communications</td>
<td>0.328</td>
<td>0.521</td>
<td>10</td>
<td>1.521</td>
<td>9</td>
</tr>
<tr>
<td>Transportation</td>
<td>0.075</td>
<td>0.824</td>
<td>8</td>
<td>1.824</td>
<td>7</td>
</tr>
<tr>
<td>Construction</td>
<td>-0.017</td>
<td>0.401</td>
<td>11</td>
<td>1.000</td>
<td>12</td>
</tr>
</tbody>
</table>
Table 3. Firm reactivity and number of operational risks hedged

This table presents the multivariate ordered probit regressions that explain the number of operational risk a firm hedges. Reactivity is calculated as the $\gamma_i$ coefficient in the regression
\[
\Delta P_{it} = \alpha_i + \gamma_i \Delta \theta_t + \varepsilon_{it},
\]
where $\Delta \theta_t$ is the annual variation in the market price of risk and $\Delta P_{it}$ is calculated as $\sqrt{(SCOR_{it} - SCOR_{i,t-1})^2 + (CF_{it} - CF_{i,t-1})^2/V_{it}}$. Business segments is the number of segments a firm operates in as reported in Compustat. Log(Assets) is the natural logarithm of total assets of the firm. Dividend Yield is the dividend paid for the year by the firm divided by its stock price. MarketValue/BookValue is calculated as the market value of the firm’s equity (stock price times the number of issued shares) divided by its book value. Long-term Debt/MarketValue is calculated as the value of the long-term debt divided by the market value of the firm (market value of equity plus book value of debt). R&D/Assets is calculated as research and development expenses divided by the total assets of the firm. Quick Ratio is the value of the currents assets minus the inventories divided by current liabilities. Foreign Sales Share is the percentage of the foreign sales over the total sales of the firm. NOL carryforward / Assets is calculated as the net operating losses carryforward divided by the firm’s total assets. Log(Managerial Stock) is the natural logarithm of the stocks market value holdings of the top five managers. Log(Managerial Option) is the natural logarithm of the options market value holdings of the top five managers.

<table>
<thead>
<tr>
<th></th>
<th>Predicted Sign</th>
<th>Without Industry Controls</th>
<th>With Industry Controls</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td>Coefficient</td>
<td>Pvalue</td>
</tr>
<tr>
<td>Reactivity</td>
<td>+</td>
<td>25.1009</td>
<td>0.005</td>
</tr>
<tr>
<td>Business Segments</td>
<td>+</td>
<td>0.0890</td>
<td>0.040</td>
</tr>
<tr>
<td>Log(Assets)</td>
<td>+</td>
<td>0.2986</td>
<td>0.002</td>
</tr>
<tr>
<td>Dividend Yield</td>
<td>+</td>
<td>-0.0033</td>
<td>0.168</td>
</tr>
<tr>
<td>Market Value / Book Value</td>
<td>+</td>
<td>-0.0007</td>
<td>0.591</td>
</tr>
<tr>
<td>LT Debt/Market Value</td>
<td>+</td>
<td>-0.0084</td>
<td>0.412</td>
</tr>
<tr>
<td>R&amp;D/Assets</td>
<td>+</td>
<td>0.0464</td>
<td>0.983</td>
</tr>
<tr>
<td>Quick Ratio</td>
<td>-</td>
<td>-0.0902</td>
<td>0.203</td>
</tr>
<tr>
<td>Foreign Sales Share</td>
<td>+</td>
<td>1.3793</td>
<td>0.000</td>
</tr>
<tr>
<td>NOL carryforward/Assets</td>
<td>+</td>
<td>2.0544</td>
<td>0.043</td>
</tr>
<tr>
<td>Log (Managerial Share)</td>
<td>+</td>
<td>-0.0527</td>
<td>0.319</td>
</tr>
<tr>
<td>Log (Managerial Option)</td>
<td>-</td>
<td>-0.0447</td>
<td>0.464</td>
</tr>
<tr>
<td>Pseudo R-square</td>
<td></td>
<td>0.1225</td>
<td></td>
</tr>
</tbody>
</table>
Figure 1: Production and operation management (POM), real risk management (RRM) and financial risk management (FRM) in the firm.
Figure 2: Efficient frontier given the portfolio of projects available to the firm.
Figure 3: Efficient frontier and value maximization of the firm given the price of risk.

\[
\frac{\Delta y}{\Delta x} = \frac{E(R_m)-R_f}{\sigma_m}
\]
Figure 4: Coordination problems.
Figure 5: Value of financial risk management.
Figure 6: The value of using financial instruments for a firm constrained by CaR requirements.
Figure 7: Impact of a change in the market price of risk on low and high concavity frontiers.
Figure 8: Number of Operational Risks Hedged as a Function of Reactivity by Industry.